USN

Fifth Semester B.E. Degree Examination, December 2010

Digital Signal Processing

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART - A

a. Derive the DFT expression from the DTFT expression.

(05 Marks)

- b. A 498 point DFT of a real valued sequence x(n) has the following DFT samples given by: X(0) = 2, X(11) = 7 + j3.1, $X(K_1) = -2.2 j1.5$, X(112) = 3 + j0.7, $X(K_2) = -4.7 + j1.9$, X(249) = 2.9, X(309) = -4.7 j1.9, $X(K_3) = 3 j0.7$, X(412) = -2.2 + j1.5 and $X(K_4) = 7 j3.1$. The other samples have a value zero. Find the value of K_1 , K_2 , K_3 and K_4 . (05 Marks)
- c. Find the 4-point DFTs of the two sequences x(n) and y(n) using a single 4-point DFT: x(n) = (1, 2, 0, 1) y(n) = (2, 2, 1, 1) (10 Marks)
- 2 a. Let $x_p(n)$ be a periodic sequence with fundamental period N. If the N point DFT $(x_p(n)) = X_1(K)$ and 3N point DFT $(xp(n)) = X_3(K)$:
 - Find the relationship between $X_1(K)$ and $X_3(K)$

ii) Verify the above result for $\{2, 1\}$ and $\{2, 1, 2, 1, 2, 1\}$ (10 Marks)

- b. For the two sequences $x_1(n) = (2, 1, 1, 2)$ and $x_2(n) = (1, -1, -1, 1)$, compute the circular convolution using DFT and IDFT. (10 Marks)
- 3 a. Let x(n) = (1, 2, 3, 4) with X(K) = (10, -2+2j, -2, -2-2j). Find the DFT of $x_1(n) = (1, 0, 2, 0, 3, 0, 4, 0)$ without actually calculating the DFT. (06 Marks)
 - b. For: $\begin{cases} x(n) = 1 & 0 \le n \le 5, \\ = 0 & \text{otherwise}. \end{cases}$

let X(Z) be the Z transform of x(n). If X(Z) is sampled at

$$Z = e^{j\binom{2\pi}{4}K} \qquad 0 \le K \le 3$$

Sketch y(n) obtained as IDFT of X(K).

(06 Marks)

c. Derive the Radix-2 algorithm for DIT-FFT for N = 8.

(08 Marks)

- 4 a. Find the 8 point DFT of {2, 1, 2, 1} using DIF FFT. Draw the signal flow graph for N = 8 with intermediate values, Stuff appropriate zeros. (10 Marks)
 - b. Find the output y(n) of a filter whose impulse response is h(n) = (1, -2, 1) and input signal x(n) = 3, 1, -2, 1, -1, 2, 4, 3, 6. Use a 8 point circular convolution using overlap-add method. (06 Marks)
 - c. Compute the IDFT of X(K) = (2, 0, 2, 0) using DIT-FFT. Use a 4 point DFT. (04 Marks)

PART - B

5 a. Derive the expression for N order of the fifth and cut-off frequency Ω_c for a lowpass Butterworth filter starting from the frequency domain specifications of a lowpass filter.

(08 Marks)

- 5 b. Design an IIR digital filter using bilinear transformation. Use Chebyshev prototype to satisfy the following specifications:
 - i) LPF with -2 dB cut-off at 100 Hz
 - ii) Stopband attenuation of 20 dB or greater at 500 Hz
 - iii) Sampling rate of 4000 samples/sec.

(12 Marks)

- 6 a. Design an analog bandpass filter to meet the following frequency domain specifications:
 - i) -3.0103 dB upper and lower cut-off frequency of 50 Hz and 20 KHz.
 - ii) A stopband attenuation of atleast 20 dB at 20 Hz and 45 KHz.
 - iii) Monotonic frequency response.

(10 Marks)

- b. Find the poles of the polynomial of order 5. Find $H_5(S)$ and gain at $\Omega = 1$ rad/sec in dB, for a Butterworth filter. (10 Marks)
- 7 a. List the steps in the design procedure of a FIR filter using window functions. (06 Marks)
 - b. A low pass filter is to be designed with the following desired frequency response:

$$\mathbf{H_d}(\mathbf{e}^{\mathbf{j}\boldsymbol{\omega}}) = \mathbf{H_d}(\boldsymbol{\omega}) = \begin{cases} \mathbf{e}^{-\mathbf{j}\boldsymbol{\omega}} & |\boldsymbol{\omega}| < \frac{\pi}{4} \\ 0 & \frac{\pi}{4} < |\boldsymbol{\omega}| < \pi \end{cases}$$

Determine the filter coefficients $h_d(n)$ and h(n) if W(n) is a rectangular window defined as :

$$\mathbf{W}_{\mathbf{R}}(\mathbf{n}) = \begin{cases} 1 & 0 \le \mathbf{n} \le 4 \\ 0 & \text{otherwise} \end{cases}$$

Also find the frequency response $H(\omega)$ of the FIR filter.

(10 Marks)

c. List the advantages and disadvantages of a FIR filter.

(04 Marks)

8 a. Obtain the cascade and parallel form realization of:

$$H(Z) = \frac{1 + \frac{1}{4}Z^{-1}}{\left(1 + \frac{1}{2}Z^{-1}\right)\left(1 + \frac{1}{2}Z^{-1} + \frac{1}{4}Z^{-2}\right)}$$
(12 Marks)

b. Realize the linear phase FIR filter having the following impulse response:

$$h(n) = \delta(n) + \frac{1}{4}\delta(n-1) - \frac{1}{8}\delta(n-2) + \frac{1}{4}\delta(n-3) + \delta(n-4)$$
 (08 Marks)

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